e01 – Interpolation

# NAG Library Function Document

# nag 2d shep eval (e01shc)

# 1 Purpose

nag\_2d\_shep\_eval (e01shc) evaluates the two-dimensional interpolating function generated by nag 2d shep interp (e01sgc) and its first partial derivatives.

# 2 Specification

```
#include <nag.h>
#include <nage01.h>

void nag_2d_shep_eval (Integer m, const double x[], const double y[],
        const double f[], const Integer iq[], const double rq[], Integer n,
        const double u[], const double v[], double q[], double qx[],
        double qy[], NagError *fail)
```

# 3 Description

nag\_2d\_shep\_eval (e01shc) takes as input the interpolant Q(x,y) of a set of scattered data points  $(x_r, y_r, f_r)$ , for r = 1, 2, ..., m, as computed by nag\_2d\_shep\_interp (e01sgc), and evaluates the interpolant and its first partial derivatives at the set of points  $(u_i, v_i)$ , for i = 1, 2, ..., n.

nag 2d shep\_eval (e01shc) must only be called after a call to nag 2d shep\_interp (e01sgc).

This function is derived from the function QS2GRD described by Renka (1988).

## 4 References

Renka R J (1988) Algorithm 660: QSHEP2D: Quadratic Shepard method for bivariate interpolation of scattered data *ACM Trans. Math. Software* **14** 149–150

## 5 Arguments

 $\begin{array}{lll} 1: & \textbf{m} - \text{Integer} & & \textit{Input} \\ 2: & \textbf{x}[\textbf{m}] - \text{const double} & & \textit{Input} \\ 3: & \textbf{y}[\textbf{m}] - \text{const double} & & & \textit{Input} \\ 4: & \textbf{f}[\textbf{m}] - \text{const double} & & & \textit{Input} \end{array}$ 

On entry:  $\mathbf{m}$ ,  $\mathbf{x}$ ,  $\mathbf{y}$  and  $\mathbf{f}$  must be the same values as were supplied in the preceding call to nag 2d shep interp (e01sgc).

5:  $iq[(2 \times m + 1)]$  - const Integer Input

On entry: must be unchanged from the value returned from a previous call to nag\_2d\_shep\_interp (e01sgc).

6:  $\mathbf{rq}[(\mathbf{6} \times \mathbf{m} + \mathbf{5})] - \text{const double}$  Input

On entry: must be unchanged from the value returned from a previous call to nag\_2d\_shep\_interp (e01sgc).

7:  $\mathbf{n}$  - Integer Input

On entry: n, the number of evaluation points.

Constraint:  $\mathbf{n} \geq 1$ .

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8:  $\mathbf{u}[\mathbf{n}]$  - const double
9:  $\mathbf{v}[\mathbf{n}]$  - const double
Input

On entry: the evaluation points  $(u_i, v_i)$ , for i = 1, 2, ..., n.

10:  $\mathbf{q}[\mathbf{n}]$  – double

On exit: the values of the interpolant at  $(u_i, v_i)$ , for i = 1, 2, ..., n. If any of these evaluation points lie outside the region of definition of the interpolant the corresponding entries in  $\mathbf{q}$  are set to the largest machine representable number (see nag\_real\_largest\_number (X02ALC)), and nag 2d shep eval (e01shc) returns with **fail.code** = NE BAD INTERPOLANT.

11:  $\mathbf{qx}[\mathbf{n}]$  - double

12:  $\mathbf{qy}[\mathbf{n}]$  - double

Output

On exit: the values of the partial derivatives of the interpolant Q(x,y) at  $(u_i,v_i)$ , for  $i=1,2,\ldots,n$ . If any of these evaluation points lie outside the region of definition of the interpolant, the corresponding entries in  $\mathbf{q}\mathbf{x}$  and  $\mathbf{q}\mathbf{y}$  are set to the largest machine representable number (see nag\_real\_largest\_number (X02ALC)), and nag\_2d\_shep\_eval (e01shc) returns with  $\mathbf{fail.code} = \mathrm{NE} \ \mathrm{BAD} \ \mathrm{INTERPOLANT}$ .

13: fail – NagError \* Input/Output

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

# 6 Error Indicators and Warnings

## NE ALLOC FAIL

Dynamic memory allocation failed.

See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

#### NE BAD INTERPOLANT

On entry, at least one evaluation point lies outside the region of definition of the interpolant. At all such points the corresponding values in  $\mathbf{q}$ ,  $\mathbf{q}\mathbf{x}$  and  $\mathbf{q}\mathbf{y}$  have been set to nag\_real\_largest\_number =  $\langle value \rangle$ .

#### **NE BAD PARAM**

On entry, argument  $\langle value \rangle$  had an illegal value.

## NE INT

On entry,  $\mathbf{m} = \langle value \rangle$ . Constraint:  $\mathbf{m} \geq 6$ . On entry,  $\mathbf{n} = \langle value \rangle$ . Constraint:  $\mathbf{n} > 1$ .

#### NE INTERNAL ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

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## NE INVALID ARRAY

On entry, values in **iq** appear to be invalid. Check that **iq** has not been corrupted between calls to nag 2d shep interp (e01sgc) and nag 2d shep eval (e01shc).

On entry, values in **rq** appear to be invalid. Check that **rq** has not been corrupted between calls to nag 2d shep interp (e01sgc) and nag 2d shep eval (e01shc).

## NE NO LICENCE

Your licence key may have expired or may not have been installed correctly. See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

# 7 Accuracy

Computational errors should be negligible in most practical situations.

## 8 Parallelism and Performance

nag\_2d\_shep\_eval (e01shc) is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

## **9** Further Comments

The time taken for a call to nag\_2d\_shep\_eval (e01shc) will depend in general on the distribution of the data points. If  $\mathbf{x}$  and  $\mathbf{y}$  are approximately uniformly distributed, then the time taken should be only O(n). At worst O(mn) time will be required.

## 10 Example

See Section 10 in nag 2d shep interp (e01sgc).

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